

SMP 3 - Construct Viable Arguments and Critique the Reasoning of Others

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- 1 SMP 3—Construct viable arguments and critique the reasoning of others—emphasizes the importance
- 2 of mathematical discourse, specifically argumentation, in the classroom.
- 3 Teachers who engage students in this practice create opportunities for them to explain, justify, and
- 4 challenge mathematical thinking. This might involve:
- Encouraging students to verbalize their thought processes when problem solving.
- Inviting students to articulate agreement or disagreement with each others' ideas or strategies.
- Sharing multiple solution strategies and asking students to compare and contrast the reasoning
 of each.
- Asking students to evaluate mathematics statements as always, sometimes, or never true, and
 prompting them to justify their reasoning.
- 11 Mathematically proficient students make conjectures, analyze situations, and build logical progressions
- 12 of statements to explore whether or not their hypotheses hold true in a variety of situations or contexts.
- 13 They justify their conclusions, communicate their reasoning to others, and respond to counterexamples.
- 14 In elementary classrooms, students may construct arguments using concrete examples such as
- 15 objects, drawings, and diagrams. For example, in this first grade standard, students are expected to
- 16 apply properties of operations and the relationship between addition and subtraction to add and
- 17 subtract. As students explore these operations, they may begin to generalize the commutative property
- 18 through reasoning and discussion.
- 19 For example, a student might use a story context about batches of cookies to explore these ideas.





- 20 Upon discussion of the context, a student might explain: Switching two piles of cookies doesn't change
- 21 how many there are in total. But giving a friend two cookies from a plate of four is not the same as
- 22 giving them four cookies from a plate of two.
- 23 Through these conversations, students may develop a deeper understanding of the commutative
- 24 property of addition while refining their ability to construct arguments and critique reasoning—key skills
- 25 to support mathematical proficiency.
- 26 Engaging in SMP 3 helps students become confident mathematical thinkers who can justify their
- 27 reasoning, refine their ideas based on evidence, and make sense of and critique the reasoning of
- 28 others. Encouraging this type of discourse in the classroom fosters a learning environment where
- 29 students see mathematics as something to be explored, discussed, and understood—not just solved.